

Exercise 40

Determine the infinite limit.

$$\lim_{x \rightarrow 2^-} \frac{x^2 - 2x}{x^2 - 4x + 4}$$

Solution

Rewrite the given limit.

$$\lim_{x \rightarrow 2^-} \frac{x(x-2)}{(x-2)^2}$$

$$\lim_{x \rightarrow 2^-} \frac{x}{x-2}$$

Since x goes to 2 from the left, the numerator is positive and the denominator is negative. Therefore,

$$\lim_{x \rightarrow 2^-} \frac{x^2 - 2x}{x^2 - 4x + 4} = -\infty.$$

